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Experimental and numerical investigations of rock-concrete interfacial crack propagation under mixed mode I-II fracture

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Abstract

Experimental tests were conducted on the composite rock-concrete specimens with four roughness profiles to investigate the propagation process of interfacial cracks under three-point bending and four-point shear conditions. By measuring the initial fracture loads, various combinations of interfacial stress intensity factors (SIFs) of modes I and II corresponding to the initial fracture conditions were determined. Based on these results, an expression for classifying the initiation of interfacial cracks under the mixed mode I-II fracture was derived by normalization, which could eliminate the effect of interfacial roughness. Furthermore, a criterion for specifying the propagation of the interfacial crack by considering the nonlinear interfacial characteristics was proposed, which indicates that the crack would start to propagate along the interface when the SIFs caused by the external loads and the cohesive stresses satisfied this criterion. The numerical simulations on the interfacial fracture process were also conducted by introducing the crack propagation criterion to predict the load versus crack mouth opening displacement ($P$-CMOD) curves, and a fairly good agreement with the experimental results could be obtained. Finally, by combining the criterion for the maximum circumferential stress with the proposed criterion for crack propagation, the interfacial crack propagation mode was assessed. The results indicated that once the initial fracture toughnesses for the rock, concrete and interface from experimental work were obtained, the propagation process of the interfacial cracks and the corresponding fracture modes including nonlinear characteristics of the materials and interface could be predicted by using the method derived in this study.

Authors’ keywords: rock-concrete interface; interface fracture; fracture mode; crack propagation criterion; initial fracture toughness.
Introduction

The operational safety of concrete gravity hydraulic dams is often threatened by the interfacial cracks between the concrete dams and the rock foundations, which are generally caused by the initial defects during construction or complex loading and environmental effects during service. The propagation of these interfacial cracks under hydrostatic pressure will decrease the load-carrying capacity and result in fracture and failure of the structures. In particular, various propagation paths of the interfacial cracks determine failure patterns of concrete dams on rock foundations. Therefore, it is significantly important to predict the fracture process and potential crack trajectory to ensure safety, serviceability and durability of a mass concrete hydraulic dam under service loading conditions.

For a rock-concrete interfacial crack, there are generally three potential propagation paths: (i) propagating fully along the interface until the structure fails; (ii) propagating first along the interface and then kinking into one material; and (iii) kinking into one material after it initiates. It has been verified by experiment that the interfacial crack may follow Path 1 at a low mode mixity ratio $K_2/K_1$ (Zhong et al. 2014) and is prone to Paths 2 and 3 at a high $K_2/K_1$ ratio (Slowik et al. 1998). Here, $K_1$ and $K_2$ are the stress intensity factors (SIFs) for fracture modes I and II at the tip of an interfacial crack, respectively. However, the crack propagation path is governed not only by the magnitude in the stress field of the crack tip, but also by the material and interface properties. Therefore, for the purpose of the fracture analysis, a criterion for interfacial crack propagation, which can evaluate the balance between the effects of the external loads and the resistance of the materials or interface, should be developed.

So far, a number of criteria have been proposed for the fracture at rock-concrete interface, classified as stress-based (Červenka et al. 1998), energy-based (Qian and Sun 1998, Sujatha and

For a small fracture process zone (FPZ) at the crack tip, linear elastic fracture mechanics (LEFM) was often employed to establish the criterion and analyze the fracture behavior at the rock-concrete interface (Červenka et al. 1998, Qian and Sun 1998, Sujatha and Kishen 2003, Kishen and Singh 2001, Yang et al. 2008). From a practical point of view, the simplification by disregarding the FPZ is acceptable for a mega structure, e.g. a gravity concrete hydraulic dam on the rock foundation. However, to investigate the fracture mechanism of the bi-material interface, the criterion based nonlinear fracture theory will be more appropriate for assessing the effect of the FPZ on fracture behavior. Particularly, due to the cohesive action on the FPZ, the stress field at the tip of an interfacial crack will change, resulting in transformation of the crack path. In addition, in the case of low mode mixity ratio, the propagation of an interfacial crack was treated as pure mode I fracture. Consequently, the mode I dominated criterion was used to determine crack propagation by assuming the crack path along the interface (Zhong et al. 2014, Dong et al. 2016a). In fact, the propagation of an interfacial crack under mixed mode I-II stress conditions can be predicted by using the formulas including fracture parameters for modes I and II (Slowik et al. 1998). The interface resistance will be over-estimated if only mode I parameter is utilized. Finally, it should be mentioned that some interface fracture criteria were derived only for homogeneous materials, i.e. the maximum circumferential stress (Ryoji and Xu 1992), the net SIF (Moës and Belytschko 2002), and the initial fracture toughness (Dong et al. 2013, Wu et al. 2013). There is a remarkable knowledge gap in the criteria for fracture and failure in homogenous materials and at bi-material interfaces. Hence, a criterion based on the fracture experiment at rock-concrete interface may be more appropriate for fracture analysis of mass concrete structures on rock foundations.
For cementation materials like concrete, the complete fracture process includes three stages: crack initiation, stable propagation and unstable propagation (Xu and Reinhardt 1999a, 1999b). These stages are also applicable for the interface fracture (Dong et al. 2016b). Regarding the cohesive effect on the FPZ under external loading, each step of the propagation of the fictitious crack can be taken as the initiation of a new crack, so that a complete fracture process consists of formations of many new cracks. A criterion used for determining the initiation of a crack can be utilized in the analysis on the crack propagation by introducing the cohesive force acting on the FPZ. This idea has been verified by the numerical simulations of the mode I fracture and mixed I-II fracture of concrete (Dong et al. 2013, Wu et al. 2013). It should be noted that the initiation and propagation of the crack in concrete is still governed by the tensile resistance although the crack tip is under a mixed mode I-II stress state. In these studies, only the initial fracture toughness of mode I was introduced as a material property. However, the scenario is different in the case of the rock-concrete interface under the mixed mode I-II fracture, because the interface is much weaker than the materials on both sides of the crack. Under this condition, the crack is prone to propagating along the interface, rather than being mode I dominated. Therefore, it is a challenge to explore what stress conditions can cause an interfacial crack to propagate, and to predict whether the crack can branch from the interface and kink into a material on one side of the interface.

The objective of this study, therefore, is to develop a criterion for predicting the propagation of the rock-concrete interfacial crack based on the initial fracture toughness and determining potential paths for the propagation of the crack. First, composite rock-concrete specimens with four interfacial roughness profiles are to be tested under three-point bending (TPB) and four-point shear (FPS). By adjusting the loading position in FPS, a wide range of $K_2/K_1$ ratios corresponding to the initial
cracking load can be obtained. A criterion for specifying the propagation of an interfacial crack based on the initial fracture toughness will then be derived by analyzing the experimental data. Thereafter, the criterion is to be employed in the numerical simulation on the interface fracture and verified by comparing the numerical results with the experimental data. Finally, combining the criterion with the material properties on both sides of the interface, potential crack propagation paths can be determined. It is expected that this investigation is to provide a better understanding of the fracture mechanism for the rock-concrete interface so that the load-carrying capacity and the serviceability and durability of mass concrete structures on rock foundations can be evaluated more accurately.

**Experimental Program**

**Specimen preparation**

Two types of specimens were prepared for the experimental study: composite rock-concrete beams and prisms with artificially grooved surfaces for the rock sections. The dimensions of the composite beams for the TPB and FPS tests were 500 mm × 100 mm × 100 mm, while the dimensions of the prism specimens for the direct tension tests were 200 mm × 100 mm × 100 mm. In addition, in order to obtain the fracture parameters of the rock and concrete, individual rock and concrete beams of 500 mm × 100 mm × 100 mm were also prepared for the TPB tests. The geometries of the composite specimens under the TPB and FPS tests are illustrated in Figs. 1(a) and (b). Each composite beam was made up of two portions, i.e. the concrete and rock sections. In the TPB tests, the lengths of the concrete and rock sections were identical, 250 mm each. In the FPS tests, the lengths of the rock sections varied from 225 mm to 250 mm to cover a wide range of mode mixity ratios for the concrete-rock (C-R) series beams. For each composite beam, the length of the
pre-crack, $a_0$, was 30 mm. In order to achieve the pre-crack, two layers of PVC film were put at the
location of the pre-crack on the rock, where one PVC film was pasted on the surface of the rock
using glue and another one was fixed at the same position using cello tape (see Fig. 2). Then the
concrete was cast against the rock section in the mold and the PVC film fixed with cello tape could
bond well with the concrete. Before testing, the cello tape was pulled out to eliminate the bonding
effect between the two layers of the PVC film.

To obtain the surfaces with various roughness degrees between the rock and concrete, four
levels of interfacial roughness were adopted by introducing artificial groove lines on the contact
surfaces of the rock sections in this study. The groove lines were parallel to the diagonal lines of the
interfacial cross-section with a depth of 3 mm. According to the numbers of groove lines, the side
surface was equally divided, and four interfacial roughness profiles were created as 3×3, 4×4, 5×5
and 7×7, respectively, as illustrated in Figs. 3(a) to (d). The degree of roughness, $R_a$, is quantified by
using the sand-filling method (Dong et al. 2016c), and its values are listed in Table 1 where a value
of $R_a$ is the average for the composite specimens with the same artificial groove pattern. Fig. 3(e)
illustrates the values of the $R_a/M_{size}$ ratio for different roughness profiles where $M_{size}$ is the maximum
size of crushed aggregate which was 10 mm for the concrete used in this study.

The rock used for the composite beams was granite, prepared in Dalian, Liaoning Province of
China. The composite beams and prisms were fabricated by casting concrete against the rough
surfaces of the rock sections. The concrete mix design was cement : water : sand : aggregate =
1:0.60:2.01:3.74 by weight. The composite specimens were demolded one day after casting, and then
cured for 28 days in the curing chamber with a 23°C curing temperature and 90% relative humidity.
Three specimens were prepared for each loading condition and roughness profile.
The mechanical properties of the concrete and rock materials and the rock-concrete interfaces are listed in Table 1, where $E$ is the elastic modulus, $\rho$ is the density, $v$ is the Poisson’s ratio, $f_t$ is the uniaxial tensile strength, $f_c$ is the uniaxial compressive strength, $K_{\text{ini}}^I$ is the initial fracture toughness of mode I, and $G_{\text{fc}}$ is the fracture energy, respectively. It should be noted that the uniaxial tensile strength of the rock-concrete interface was obtained on the prism specimens tested in direct tension.

**TPB and FPS tests**

The composite TPB and FPS specimens with four interfacial roughness profiles were tested in a 250 kN closed-loop servo MTS testing machine at a displacement rate of 0.024 mm/min. The experimental setups for the TPB and FPS tests are illustrated in Figs. 4(a) and (b), respectively. The ratio of loads on the two loading points is 1:6 for all C-R series specimens under FPS. The displacement at the loading point, the crack mouth opening displacement ($CMOD$) and the crack mouth sliding displacement ($CMSD$) were measured using clip gauges in the test. In addition, to measure the initial cracking load, two strain gauges were symmetrically put on both sides of the specimen, 5 mm away from the tip of the pre-notch in the ligament. Once the pre-crack began to propagate, the measured strains would drop rapidly due to the sudden release of the stored strain energy at the pre-crack in the specimen. By taking Specimen C-R-240-4×4-1 as an example, Fig. 5 illustrates the relationship between the load and strain at the tip of the pre-crack. It can be seen that the strain reached its maximum at the initial cracking loading $P_{\text{ini}} = 23.32$ kN, and thereafter the strain started to decrease. The decrease in the strain indicates the release of the stored strain energy at the pre-crack tip so that the initial cracking load could be determined.

The experimental results for the TPB and FPS specimens are listed in Tables 2 and 3, respectively. The specimen number “TPB-3×3” in Table 2 denotes the TPB specimen with the 3×3
artificial groove pattern, see Fig. 1(a). $G_{II}$ in Table 2 denotes the fracture energy of mode I fracture for the interfaces with different roughness profiles. The specimen number “C-R-225-3×3” in Table 3 denotes the FPS specimen with the left and right sections as the concrete and rock, respectively. The length for the rock section was 225 mm with the 3×3 artificial groove pattern, see Fig. 1(b). Here, $P_{ini}$ and $P_{max}$ are the initial and peak loads, and $L_R$ is the length of the rock section. The stress intensity factors $K_1$ and $K_2$ for the bi-material interfacial crack were calculated using Eqs. (1) to (7) below (Nagashima et al. 2003). Here, $\delta_x$ and $\delta_y$ are the relative crack surface displacements in the horizontal x and vertical y directions. $K_1$ and $K_2$ can be written as $K_{ini}^1$ and $K_{ini}^2$ when $\delta_x$ and $\delta_y$ in Eqs. (1) and (2) are caused by the initial cracking load:

$$K_1 = C \lim_{r \to \infty} \sqrt{\frac{2\pi}{r}} \left[ \delta_x (\cos Q + 2\varepsilon \sin Q) + \delta_y (\sin Q - 2\varepsilon \cos Q) \right]$$

(1)

$$K_2 = C \lim_{r \to \infty} \sqrt{\frac{2\pi}{r}} \left[ \delta_x (\cos Q + 2\varepsilon \sin Q) - \delta_y (\sin Q - 2\varepsilon \cos Q) \right]$$

(2)

where

$$C = \frac{2 \cosh(\varepsilon\pi)}{(\kappa_1 + 1)/\mu_1 + (\kappa_2 + 1)/\mu_2}$$

(3)

$$Q = \varepsilon \ln r$$

(4)

$$\varepsilon = \frac{1}{2\pi} \ln \left( \frac{\mu_1 + 1}{\mu_2 + 1} \right)$$

(5)

$$\mu_i = \frac{E_i}{2(1+\nu_i)} \quad (i = 1, 2)$$

(6)

$$\kappa_i = \begin{cases} (3-\nu_i)/(1+\nu_i) & \text{(Plane stress)} \\ (3-4\nu_i) & \text{(Plane strain)} \end{cases}$$

(7)

$E_i$ is the elastic modulus for material $i$, $\nu_i$ is the Poisson’s ratio for material $i$, $r$ is the radius of the
pre-crack at its tip.

There are two basic failure modes for the composite C-R series beams under FPS. The interface failure mode “I” means that the interfacial crack propagates through the interface until failure occurs. Some C-R series beams which fractured in this failure mode are shown in Fig. 6(a). The other failure mode “IC” was observed on the beams with high mode mixity ratios. Fig. 6(b) shows some examples of this failure mode. In the case of the failure mode “IC”, a sudden brittle failure was observed near the supports at the same time when the interfacial crack propagated through the whole interface. In the case of the failure mode “IC”, the failure at the interior support within the concrete section of the specimen occurred during the unstable fracture process. The initial fracture toughness was calculated based on the initial cracking load, i.e. the failure at the interior support did not occur when the crack initiated. Therefore, the failure mode “IC” did not affect the determination of the initial fracture toughness in this study.

In addition, it is worthwhile to point out that the crack did not propagate exactly along the interfaces. On the artificial grooves of the rock, the crack propagated through the concrete on the grooves (see Fig. 7). For a precise computation, the discrete microstructural model, such as lattice models (Bažant et al. 1990, Gianluca et al. 2003a, 2003b, 2006, 2011a, 2011b), will be a more powerful and realistic alternative for simulating the softening damage and fracture of concrete. In these models, the concrete was sub-divided into mortar, aggregate and the interface between them, and these sub-components can be described as mesoscopic elements. Various meso-structural characteristics, such as aggregate size and distribution, and stress and strain fields in the meso-structure, can be directly simulated. In this study, the concrete was modeled as the homogeneous materials and this study was conducted from macroscopic perspectives rather than
mesoscopic ones. The interfacial fracture energy and fracture toughness reflect the fracture characteristics at the interface on average. The effect of the interfacial roughness profile is considered through measuring the fracture energy and fracture toughness of the specimens with the same degree of roughness. These fracture parameters to be used in the following numerical simulations also corresponded to those from the specimens with the same degree of roughness.

**Criterion for Crack Propagation and Experimental Verification**

**Criterion for crack propagation**

From the experimental results, it can be found that the interfacial cracks can initiate under different combinations of $K_{1}^{\text{ini}}$ and $K_{2}^{\text{ini}}$. When the interfacial fracture was pure mode I, the crack initiation would be determined by the intial mode I fracture toughness, $K_{Ic}^{\text{ini}}$, i.e. $K_{1}^{\text{ini}} = K_{Ic}^{\text{ini}}$ and $K_{2}^{\text{ini}} = 0$. When the fracture mode of interface was pure mode II, the crack initiation would be determined by the intial mode II fracture toughness, $K_{II}^{\text{ini}}$, i.e. $K_{1}^{\text{ini}} = 0$ and $K_{2}^{\text{ini}} = K_{IIc}^{\text{ini}}$. In addition, in the cases of mixed mode I-II interfacial fracture, $K_{1}^{\text{ini}} < K_{Ic}^{\text{ini}}$ and $K_{2}^{\text{ini}} < K_{IIc}^{\text{ini}}$. The mode mixity ratio, $K_{2}^{\text{ini}} / K_{1}^{\text{ini}}$, represents the relationship between the tensile and shear stresses at the tip of the interfacial crack. If all the combinations of $K_{1}^{\text{ini}}$ and $K_{2}^{\text{ini}}$ are grouped to form an envelope, it will represent the crack initiation conditions under various combinations of tensile and shear stresses. Thus, the equation for the curve with the parameters $K_{1}^{\text{ini}}$ and $K_{2}^{\text{ini}}$ would become the criterion for the initiation of a crack. Through careful experimental design, a wide range of $K_{2}^{\text{ini}} / K_{1}^{\text{ini}}$ ratios could be derived from the TPB and FPS tests, varying from 0.055 to 16.595, as illustrated Tables 2 and 3. Furthermore, the effect of the interface roughness on the criterion for the crack initiation was investigated by testing the composite specimens with four roughness profiles. Fig. 8 illustrates the
relationships between $K_{1}^{\text{ini}}$ and $K_{2}^{\text{ini}}$ from the testing data with various interface roughness degrees and the fitted curves. It can be seen that the $K_{1}^{\text{ini}}$ versus $K_{2}^{\text{ini}}$ curve would move outward when $R_{a}$ increased from 0.780 to 1.548, indicating that the interfacial cracking resistance would indeed increase with the increasing interfacial roughness.

To derive the equation for the initial fracture by eliminating the effect of roughness degree, the normalizing method was utilized by dividing $K_{1}^{\text{ini}}$ and $K_{2}^{\text{ini}}$ by the corresponding $K_{1C}^{\text{ini}}$ for each test series with the same $R_{a}$. The points for the normalized terms $K_{1}^{\text{ini}} / K_{1C}^{\text{ini}}$ and $K_{2}^{\text{ini}} / K_{1C}^{\text{ini}}$ with various values of $R_{a}$ are shown in Fig. 9. It can be seen that the effect of the interface roughness could be eliminated approximately through the normalizing process. Therefore, the regressive equation for the initial fracture could be derived by fitting all the scattered testing points as Eq. (8), where the shape of the equation for the initiation of the interfacial crack would be a quarter-ellipse, with the ratio of the long axial length to the short axial length as 1.6, i.e.

$$\left( \frac{K_{1}^{\text{ini}}}{K_{1C}^{\text{ini}}} \right)^{2} + \left( \frac{K_{2}^{\text{ini}}}{1.6 K_{1C}^{\text{ini}}} \right)^{2} = 1 \quad (8)$$

If a complete fracture process could be regarded as crack propagation for many steps, each step for the propagation of the existing crack would be regarded as the initiation of a new crack. Then, the crack initiation equation could be used to predict the crack propagation at interface. However, considering the nonlinear characteristics of the rock-concrete interface, there are cohesive stresses acting on the FPZ of the interfacial crack according to the fictitious cracking model (Hillerborg et al. 1976). Therefore, when the equation for the crack initiation was used to predict the propagation process of the crack, the SIFs, $K_{1}$ and $K_{2}$, would be governed by the external load and the cohesive force of the PFZ, i.e. $K_{1} = K_{1}^{p} - K_{1}^{\sigma,\tau}$ and $K_{2} = K_{2}^{p} - K_{2}^{\sigma,\tau}$. Here, $K_{1}^{p}$ and $K_{2}^{p}$ are the SIFs of modes I and II caused by the external load, while $K_{1}^{\sigma,\tau}$ and $K_{2}^{\sigma,\tau}$ are the SIFs of modes I and II.
caused by the cohesive tensile and shear stresses on the FPZ, \( \sigma \) and \( \tau \). Thus, Eq. (8) can be rewritten as Eq. (9) when it is used to determine the propagation of the crack along the interface, with \( K_{1,2}^* \) representing the function of the criterion for the propagation of the interfacial crack:

\[
K_{1,2}^* = \sqrt{\left( \frac{K_1^p - K_1^{\sigma}}{1} \right)^2 + \left( \frac{K_2^p - K_2^{\sigma}}{1.6} \right)^2} = K_{IC}^{ini}
\]  

In the case of mode I interface fracture, \( K_2 \) and the cohesive shear stress are equal to 0 so that Eq. (9) will be degenerated to:

\[
K_1^p - K_1^{\sigma} = K_{IC}^{ini}
\]  

Eq. (10) is the criterion of the crack propagation for the mode I interface fracture, which is a particular case of the mixed mode I-II fracture and has been verified in the previous research (Dong et al. 2016a).

**Application and experimental verification**

In order to verify the derived criterion for the propagation of the interfacial crack, numerical simulations based on the fictitious cracking model were conducted to predict the fracture process of the composite rock-concrete beams under TPB and FPS. The finite element analyses were carried out using commercial software ANSYS. The cohesive traction-displacement relationships for tension and shear softening are illustrated in Figs. 10(a) and (b), respectively. In Fig. 10(a), the crack opening displacement (COD) at the breaking point on the bi-linear \( \sigma \)-\( w \) curve, \( w_{n0} \), and the corresponding cohesive stress, \( \sigma_{n0} \), were set as 0.8\( G_{II}/f_t \) and 0.2\( f_t \), respectively. The stress-free COD, \( w_{nc} \), was set as 6\( G_{II}/f_t \) (Dong et al. 2016c). In Fig. 10(b), the crack slip displacement (CSD) at the breaking point on the bi-linear \( \tau \)-\( w \) curve, \( w_{s0} \), and the corresponding interface shear strength, \( \tau_{s0} \), were set as 0.002 mm and 7\( f_t/4 \), respectively. The stress-free CSD, \( w_{sc} \), was set as 2\( G_{II}/\tau_{s0} \). Here, \( G_{II} \) is the mode II interface fracture energy, which was set to be equal to 2\( G_{II} \) (Zhong et al. 2014).
If a pre-crack is assumed to initiate and propagate fully along the interface, the criterion for the crack propagation can be used to predict the complete fracture process under the mixed mode I-II fracture. Fig. 11 illustrates the flow chart for the program, and the numerical simulation procedure is summarized as follows:

1. Establish the finite element model with the crack length \( a_{ij} = a_0 + (j - 1) \Delta a \) \((i = 1, 2; j = 2, 3\ldots)\). Here \( a_0 \) is the initial crack length, \( \Delta a \) is a specified increment of the crack length, \( i \) represents the load increment during the iteration process with a fixed crack length, and \( j \) represents the increment of the crack length during the iterations.

2. Apply the load \( P_{ij} \) and calculate the cohesive stresses \( \sigma_{ij} \) and \( \tau_{ij} \) according to the cohesive tensile/shear traction – displacement relationships as shown in Fig. 10.

3. Calculate \( K_1^p \), \( K_2^0 \), \( K_1^{\alpha,r} \) and \( K_2^{0,\tau} \) by adjusting load \( P_{ij} = P_{i-1,j} \pm \Delta P \) until Eq. (9) is satisfied.

4. Repeat Steps 1 and 3 for the next step of crack propagation.

5. Terminate the iterative process when \( a_{ij} \) is equal to the specimen height or \( P_{ij} \leq 0 \).

By repeating the steps, the complete interface fracture process can be obtained numerically. The parameters used in the simulations included \( K_1^{\text{int}} \) and \( G_{\text{It}} \), which have been listed in Tables 1 and 2.

By taking Specimens TPB-5×5, C-R-240-3×3, C-R-240-4×4, C-R-235-5×5 and C-R-250-7×7 as examples, Fig. 12 illustrates the comparisons of the numerically predicted \( P-CMOD \) curves with the experimental data, and fairly good agreements can be observed.

**Discussion on Crack Propagation Paths**

As motioned above, three potential propagation paths existed for the pre-crack at the
rock-concrete interface, which would be governed by the stress conditions in front of the crack tip and the mechanical properties of the concrete, rock and their interface. Generally, the mechanical and fracture properties of the interface were smaller than those for the concrete and rock. Therefore, the crack would propagate along the interface in the mode I dominated fracture. With the increase of $K_2/K_1$, the crack could branch at the interface and kink into the rock or concrete, even the crack directly initiated in the rock or concrete. To predict the potential crack propagation path, in addition to the criterion for the propagation of the interfacial crack, it is also essential to develop the criterion for the crack to penetrate into the rock or concrete.

In this study, the function for the maximum circumferential stress criterion (Ryoji and Xu 1992, Kishen and Singh 2001) was employed to determine the kinking of the interfacial crack as follows:

$$K_{i,j}^* = \sqrt{\left(K_{i,j}^a - K_{i,j}^{a,i}\right)^2 + \left(K_{i,j}^p - K_{i,j}^{p,i}\right)^2} \cdot W_j \left[ 2 \cos \left( \frac{\theta_0}{2} + \gamma \right) - \left( \cos \theta_0 + 2\varepsilon \sin \theta_0 \right) \cos \left( \frac{\theta_0}{2} - \gamma \right) \right] + \frac{1}{W_j} \cos \left( \frac{3}{2} \theta_0 + \gamma \right) = K_{i,j}^{\text{ini}}$$

(11)

where $K_{i,j}^{\text{ini}}$ is the initial mode I fracture toughness of material $j$, $j$ denotes rock or concrete, and $\theta_0$ is the kinking angle which can be obtained by solving Eq. (12) numerically

$$\varepsilon W_j \left[ 2 \cos \left( \frac{\theta_0}{2} + \gamma \right) - \left( \cos \theta_0 + 2\varepsilon \sin \theta_0 \right) \cos \left( \frac{\theta_0}{2} - \gamma \right) \right]$$

$$+ W_j \left[ -\sin \left( \frac{\theta_0}{2} + \gamma \right) + \left( \sin \theta_0 - 2\varepsilon \cos \theta_0 \right) \cos \left( \frac{\theta_0}{2} - \gamma \right) \right]$$

$$+ W_j \left[ \frac{1}{2} \left( \cos \theta_0 + 2\varepsilon \sin \theta_0 \right) \sin \left( \frac{\theta_0}{2} - \gamma \right) - \frac{1}{W_j} \left[ \varepsilon \cos \left( \frac{3}{2} \theta_0 + \gamma \right) + \frac{3}{2} \sin \left( \frac{3}{2} \theta_0 + \gamma \right) \right] = 0 \right]$$

(12)

with

$$\gamma = \begin{cases} \arctan((K_{i,j}^p/K_{i,j}^{p,i})) & K_1 > 0 \\
\pi + \arctan((K_{i,j}^p/K_{i,j}^{p,i})) & K_1 < 0 \end{cases}$$

(13)

$$W_j = \begin{cases} e^{\varepsilon (\pi - \theta_0)} & j = 1 \\
\varepsilon^{\varepsilon (\pi - \theta_0)} & j = 2 \end{cases}$$

(14)

It should be mentioned that the expression for the maximum circumferential stress criterion
used in this study is different from those in literature (Ryoji and Xu 1992, Kishen and Singh 2001).

Instead of the unstable fracture toughness $K_{ICj}$, the initial fracture toughness $K_{ij}^{ini}$, which is on the right side of Eq. (11) was used to determine the crack initiation. The purpose of the substitution is considering that the crack propagation into the material $j$ still represents the initiation of a new crack rather than the unstable propagation of the existing crack. In addition, Eq. (11) can only be obtained for small $|\varepsilon|$ (Ryoji and Xu 1992). Here, $\varepsilon$ is a material constant shown in Eq. (5). Fortunately, the value of $|\varepsilon|$ for dissimilar composite materials is less than 0.1. For instance, the value of $|\varepsilon|$ for the composite rock-concrete specimens in this study was calculated as 0.0074, so that the criterion shown in Eq. (11) should be valid.

By combining the criterion equation for the propagation of the interfacial crack, i.e. Eq. (9), with the criterion equation for the maximum circumferential stress of material $j$, i.e. Eq. (11), the potential propagation of an interfacial crack could be judged in this study as follows:

(i) If $K_{IIIj}^{*} < K_{ij}^{ini}$ and $K_{1,2}^{*} < K_{1C}^{ini}$, the crack does not propagate;

(ii) If $K_{IIIj}^{*} < K_{ij}^{ini}$ and $K_{1,2}^{*} > K_{1C}^{ini}$, the crack propagates along the interface;

(iii) If $K_{IIIj}^{*} > K_{ij}^{ini}$ and $K_{1,2}^{*} < K_{1C}^{ini}$, the crack propagates into the material $j$ with a kinking angle $\theta_0$.

The above mentioned method can be also used to predict the crack initiation. In this case, only the SIFs caused by the external load, i.e. $K_1^{p}$ and $K_2^{p}$, exist in the expressions for $K_{IIIj}^{*}$ and $K_{1,2}^{*}$, due to no development of micro-cracks. Therefore, the crack will directly penetrate into the material $j$ if $K_{IIIj}^{*} > K_{ij}^{ini}$ and $K_{1,2}^{*} < K_{1C}^{ini}$. Under this condition, the fracture analysis transforms into the crack propagation in a homogeneous material under the mixed mode I-II loading, which has been investigated by Wu et al. (2013).
In addition, the potential crack propagation path could be predicted by applying the criteria for
the propagation of the interfacial crack and the maximum circumferential stress. By taking the
composite C-R series beams in this study as examples, Fig. 13(a) shows the $K_1 - K_2$ relationships of
the criteria with $K^*_{1,II} = K^\text{ini}_I$ for the rock and $K^*_{1,2} = K^\text{ini}_{1C}$ for the interface. For the composite C-R
series beams under the loading condition as shown in Fig. 1(b), it is impossible for the crack to kink
into the concrete so that only the criterion for the interfacial crack propagation and the criterion for
the maximum circumferential stress of the rock were assessed. For the criterion for the interfacial
initiation, i.e. $K^*_1 = K^\text{ini}_1$, there were four curves with respect to the interfaces of four
roughness degrees, as illustrated in Fig. 13(a). For the criterion for the maximum circumferential
stress of the rock, i.e. $K^*_1 = K^\text{ini}_j$ with $j$ representing the rock, there is one curve illustrated in Fig.
13(a). $K^\text{ini}_j$ for the rock in this study was determined as 1.205 MPa·m$^{1/2}$ by conducting the standard
TPB tests on the rock specimens. It can be seen from this figure that the curve for the rock with
$K^*_{1,II} = K^\text{ini}_j$ is always outside the curves for $K^*_{1,2} = K^\text{ini}_{1C}$. This indicates that under any loading
conditions, the crack would not propagate into the rock from the interfaces of the composite C-R
specimens with four roughness degrees in this study. This has also been validated by the
experimental failure patterns of the composite C-R series beams as shown in Fig. 6. The qualitative
assessment is significantly useful for practical constructions, e.g. gravity concrete hydraulic dams, to
determine whether propagations of interfacial cracks into rock foundations can be excluded or not.

It should be mentioned that, even though the crack propagated fully along the interface for all
composite C-R series beams, there would still exist two different variation tendencies for $K_2/K_1$
during the complete fracture process. One is that the ratio $K_2/K_1$ would always increase as the
interfacial crack propagated, and another is that the ratio would always decrease correspondingly.
Based on the numerical simulation results, it is found that there was a critical value for the mode
mixity ratio $K_2/K_1$ when the material and interface properties were given. This critical mode mixity
ratio was equal to 0.788 for the materials adopted in this study. The points for four toughness degrees
corresponding to the critical mode mixity ratio are illustrated in Fig. 13(a) as A, B, C and D,
respectively. When the ratio $K_2^{\text{ini}}/K_1^{\text{ini}}$ was less than the critical value, the ratio $K_2/K_1$ would always
decrease as the crack propagated so that the fracture became mode I dominated. In contrast, when the
ratio $K_2^{\text{ini}}/K_1^{\text{ini}}$ was greater than the critical value, the ratio $K_2/K_1$ would always increase as the
crack propagated and the fracture became mode II dominated. Fig. 13(a) also shows the variations of
$K_2/K_1$ during the crack propagation for the C-R-235 series specimens with
$K_2^{\text{ini}}/K_1^{\text{ini}} = 0.718 < 0.788$ (see the solid symbols in Fig. 13(a)), and for the C-R-245 series
specimens with $K_2^{\text{ini}}/K_1^{\text{ini}} = 2.275 > 0.788$ (see the hollow symbols). This clearly illustrates the
variation tendencies of $K_2/K_1$ for the specimens with different values of $K_2^{\text{ini}}/K_1^{\text{ini}}$ during the
complete fracture process.

Although the interfacial crack does not propagate into the rock based on the criterion
comparisons in Fig. 13(a), the propagation path of the interfacial crack can still not be defined if the
positions of the rock and concrete are exchanged. In this case, the relationship between the criterion
for the maximum circumferential stress of the concrete and the criterion for the propagation of the
interfacial crack should be evaluated. The curves for the criteria with $K_{1,\text{II}}^{*} = K_{1j}^{\text{ini}}$ and $K_{1,2}^{*} = K_{1C}^{\text{ini}}$
are shown in Fig. 13(b), where $j$ denotes the concrete material. For the criterion with $K_{1,2}^{*} = K_{1C}^{\text{ini}}$, the
curves with respect to two toughness degrees ($R_a = 0.963$ and $K_{1C}^{\text{ini}} = 0.399$; $R_a = 1.183$,
$K_{1C}^{\text{ini}} = 0.450$) are illustrated as examples. For the criterion with $K_{1,\text{II}}^{*} = K_{1j}^{\text{ini}}$, $K_{1j}^{\text{ini}}$ for the concrete
was determined as 0.55 MPam$^{1/2}$ from the standard TPB tests on the concrete specimens. Compared
with the curves in Fig. 13(a), the criterion curve for the interface intersected with the curve for the concrete in Fig. 13(b). The intersection points corresponded to different $K_2/K_1$ ratios, i.e. $P_C = 0.764$ ($R_a = 0.963$ and $K_{ic}^{ini} = 0.399$) and $Q_C = 0.509$ ($R_a = 1.183$ and $K_{ic}^{ini} = 0.450$). This indicates that the interfacial crack would directly initiate and propagate into concrete when $K_2^{ini} / K_1^{ini} > 0.764$ for $R_a = 0.963$ and $K_2^{ini} / K_1^{ini} > 0.509$ for $R_a = 1.183$. In contrast, the interfacial crack would initiate and propagate along the interface when $K_2^{ini} / K_1^{ini} < 0.764$ for $R_a = 0.963$ and $K_2^{ini} / K_1^{ini} < 0.509$ for $R_a = 1.183$. In addition, it is worthwhile to discuss whether an interfacial crack could kink into the concrete after propagating along the interface. Based on the previous investigations, the variations in $K_2/K_1$ in the case of interfacial propagation were determined by the critical mode mixity ratio, which are marked as Points B and C in Fig. 13(b). The intersection points $Q_C$ and $P_C$ are on the left of the critical points C and B, respectively. It indicates that, in the cases of $K_2^{ini} / K_1^{ini} < 0.764$ (Point $Q_C$) for $R_a = 0.963$ and $K_2^{ini} / K_1^{ini} < 0.509$ (Point $P_C$) for $R_a = 1.183$, the $K_2/K_1$ ratio would increase as the interfacial crack propagates so that it would not propagate into the concrete under this condition.

In order to verify the crack propagation in this case, the composite rock-concrete (R-C) series beams were prepared with two interfacial roughness degrees, i.e. $R_a = 0.963$ and 1.183. The geometric properties of the R-C series specimens are shown in Fig. 14. It should be noted that, compared with the C-R series specimens shown in Fig. 1(b), the positions of the rock and concrete in the R-C series specimens were exchanged so that the crack could propagate along the interface or penetrate into the concrete under this loading condition. The $K_2^{ini}/K_1^{ini}$ ratios were determined as 0.788 and 0.696 for $R_a = 0.963$, and 0.531 and 0.437 for $R_a = 1.183$ (see Table 4). The corresponding points are denoted as $P_2$, $P_1$, $Q_2$ and $Q_1$ in Fig. 13(b), respectively. The experimental design ensured that the $K_2^{ini}/K_1^{ini}$ ratios for the test points would be on both sides of the criterion intersection points for the
The experimental results are listed in Table 4. For the R-C series specimens, the initiation and propagation of the crack in the concrete were observed on Specimens R-C-264-4×4 (Point \( P_2 \) with \( K_2^{\text{ini}} / K_1^{\text{ini}} = 0.788 \)) and R-C-271-5×5 (Point \( Q_2 \) with \( K_2^{\text{ini}} / K_1^{\text{ini}} = 0.531 \)), which is denoted as the failure mode K in Table 4. Correspondingly, the crack propagations fully along the interface were observed on Specimens R-C-266-4×4 (Point \( P_1 \) with \( K_2^{\text{ini}} / K_1^{\text{ini}} = 0.696 \)) and R-C-275-5×5 (Point \( Q_1 \) of \( K_2^{\text{ini}} / K_1^{\text{ini}} = 0.437 \)), which is denoted as the failure mode I. Fig. 15 shows the failure mode with the initiation and propagation of the crack into the concrete. By taking Specimen R-C-264-4×4 as an example, Figs. 16(a) and (b) illustrate the comparison of the \( P\text{-CMOD} \) curves and the crack propagation trajectories between the experimental and numerical results, respectively, and reasonably good agreements can be observed.

The investigations in this study indicate that the crack propagation mode under different stress conditions could be predicted by combining Eqs. (9) and (11). The application of the proposed predicting method is convenient because only three initial fracture toughnesses for the rock and concrete materials and their interface would be required in these two equations. Particularly, the three initial fracture toughnesses are relatively easily obtained from the experiment (Dong et al. 2013, Dong et al. 2016c). Once the curves for Eqs. (9) and (11) are obtained, therefore, the failure mode for a mass concrete structure on the rock foundation can be approximately assessed according the loading conditions. However, it should be noted that the further work is still needed to investigate whether Eq. (9) is appropriate for concretes and rocks with various strengths and compositions.

Conclusions

To study the propagation process of the rock-concrete interfacial crack, an expression for the
initiation of the interfacial crack has been derived from the experimental investigations. By taking into account the nonlinear characteristics of the interface between two different materials, a criterion for the crack propagation has been proposed to envisage the propagation of a crack along the interface. Based on the criterion for the maximum circumferential stress and the proposed criterion in this study, the interfacial fracture modes, including propagating of a crack along the interface and kinking into the rock or concrete, can be predicted by analyzing the verification curves for these two criteria simultaneously. According to the comprehensive experimental and numerical investigations, the following conclusions can be drawn:

1. For the rock-concrete interfaces with four different roughness profiles investigated in this study, a universal expression for predicting the initiation of a crack along the interface has been obtained by normalizing their initial fracture toughnesses. Also, a criterion for the propagation of the crack has been proposed based on the expression for the crack initiation by introducing the fictitious crack model. This criterion has been verified by comparing the $P$-$CMOD$ curves obtained numerically and experimentally, and fairly good agreements have been observed. However, further work should be conducted to verify the validity of the universal expression for the initiation of a crack at the interfaces between concrete and rock of different properties and compositions.

2. The proposed criterion for the propagation of the interfacial crack can be utilized to predict the complete interfacial fracture process for the mixed mode I-II fracture. By applying the fictitious cracking model, the nonlinear characteristics of the interface have been considered in the criterion. This has been verified by comparing the $P$-$CMOD$ curves obtained from the experimental investigations and numerical simulations. For propagation of the crack along the
interface, there exists a critical mode mixty ratio, which has been determined as 0.788 for the materials used in this study. When the $K_{2/1}^{\text{ini}} / K_{1}^{\text{ini}}$ ratio was greater than the critical mode mixty ratio, $K_{2/1}$ would increase as the interfacial crack propagated. In contrast, when the $K_{2/1}^{\text{ini}} / K_{1}^{\text{ini}}$ ratio was less than the critical mixty ratio, the $K_{2/1}$ ratio would decrease as the interfacial crack propagated.

3. Crack propagation paths, i.e. developing along the interface or kinking into the rock or concrete, could be predicted by analyzing the curves for the criterion for the interfacial crack propagation and the criterion for the crack to kink into the rock or concrete. If the curve for the interfacial criterion was inside the curve for the kinking criterion for the rock or concrete, the crack would always propagate along the interface. In contrast, if there was an intersection point between two criteria, the interfacial crack would either propagate along the interface or penetrate into rock or concrete, depending on the relationship between the $K_{2/1}^{\text{ini}} / K_{1}^{\text{ini}}$ ratio and the $K_{2/1}$ ratio corresponding to the intersection point.

4. The criteria for propagating and kinking of the interfacial crack into the rock or concrete could be determined by obtaining the initial fracture toughnesses of the rock, concrete and their interface. Actually, these values could be conveniently derived by measuring the initial fracture load from the TPB tests.

Acknowledgements

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of Liaoning Province of China under the grant of 20170540183 is gratefully acknowledged.

References


### Table 1 Mechanical properties of concrete and rock materials and their interfaces\(^1\).

<table>
<thead>
<tr>
<th>Series</th>
<th>$E$ (GPa)</th>
<th>$\rho$ (g/cm(^3))</th>
<th>$\nu$</th>
<th>$f_t$ (MPa)</th>
<th>$f_c$ (MPa)</th>
<th>$R_a$ (mm)</th>
<th>$K_{ini}^1$ (MPa·m(^{1/2}))</th>
<th>$G_{If}$ (N/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concrete</td>
<td>32.86</td>
<td>2.45</td>
<td>0.256</td>
<td>2.200</td>
<td>37.20</td>
<td>0.550</td>
<td>101.91</td>
<td></td>
</tr>
<tr>
<td>Rock</td>
<td>41.17</td>
<td>2.75</td>
<td>0.173</td>
<td>-</td>
<td>142.00</td>
<td>1.205</td>
<td>135.38</td>
<td></td>
</tr>
<tr>
<td>Interface (3×3)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1.170</td>
<td>-</td>
<td>0.780</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Interface (4×4)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1.391</td>
<td>-</td>
<td>0.963</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Interface (5×5)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1.659</td>
<td>-</td>
<td>1.183</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Interface (7×7)</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>2.101</td>
<td>-</td>
<td>1.548</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>

\(^1\)E – Elastic modulus; $\rho$ – Density; $\nu$ – Poisson's ratio; $f_t$ – Uniaxial tensile strength; $f_c$ – Uniaxial compressive strength; $R_a$ – Degree of roughness; $K_{ini}^1$ – Initial fracture toughness of mode 1; $G_{If}$ – Fracture energy.

### Table 2 Experimental results of the TPB tests\(^2\).

| Specimen | $P_{ini}$ (kN) | $P_{\text{max}}$ (kN) | $K_{ini}^1$ (MPa·m\(^{1/2}\)) | $K_{ini}^2$ (MPa·m\(^{1/2}\)) | $|K_{ini}^2/K_{ini}^1|$ | $R_a$ (mm) | $G_{If}$ (N/m) |
|----------|----------------|------------------------|--------------------------------|-------------------------------|------------------------|-----------|----------------|
| TPB-3×3  | 1.720          | 1.825                  | 0.351                          | -0.019                        | 0.055                  | 0.780     | 9.25           |
| TPB-4×4  | 1.965          | 2.234                  | 0.399                          | -0.022                        | 0.055                  | 0.963     | 18.98          |
| TPB-5×5  | 2.210          | 2.623                  | 0.450                          | -0.025                        | 0.055                  | 1.183     | 22.72          |
| TPB-7×7  | 2.385          | 2.816                  | 0.483                          | -0.026                        | 0.055                  | 1.548     | 30.14          |

\(^2\)P$_{ini}$ – Initial cracking load; $P_{\text{max}}$ – Peak load; $K_{ini}^1$ – Initial fracture toughness of mode 1; $K_{ini}^2$ – Initial fracture toughness of mode 2; $R_a$ – Degree of roughness; $G_{If}$ – Fracture energy.
Table 3 Experimental results of the C-R series beams under FPS$^2$.

| Specimen   | $L_R$ (mm) | $P_{ini}$ (kN) | $P_{max}$ (kN) | $K_{ini}^{IC}$ (MPa·m$^{1/2}$) | $K_{ini}^{IC}$ (MPa·m$^{1/2}$) | $|K_{ini}^{IC}/K_{ini}^{IC}|$ | $R_e$ (mm) | Failure mode |
|------------|------------|----------------|----------------|--------------------------------|--------------------------------|-----------------------------|------------|--------------|
| C-R-225-3×3 | 225        | 12.860         | 14.947         | 0.399                          | 0.143                          | 0.359                       | I          |              |
| C-R-235-3×3 | 235        | 14.136         | 18.813         | 0.298                          | 0.215                          | 0.723                       | I          |              |
| C-R-240-3×3 | 240        | 22.000         | 22.545         | 0.334                          | 0.381                          | 1.138                       | 0.780      | I            |
| C-R-245-3×3 | 245        | 27.065         | 27.865         | 0.232                          | 0.528                          | 2.275                       | I          |              |
| C-R-250-3×3 | 250        | 27.500         | 37.087         | 0.036                          | 0.606                          | 16.595                      | I          |              |
| C-R-225-4×4 | 225        | 13.405         | 15.355         | 0.416                          | 0.149                          | 0.358                       | I          |              |
| C-R-235-4×4 | 235        | 17.080         | 20.687         | 0.361                          | 0.260                          | 0.719                       | I          |              |
| C-R-240-4×4 | 240        | 23.990         | 27.050         | 0.365                          | 0.415                          | 1.136                       | 0.963      | I            |
| C-R-245-4×4 | 245        | 28.898         | 33.390         | 0.248                          | 0.564                          | 2.270                       | I          |              |
| C-R-250-4×4 | 250        | 33.208         | 39.957         | 0.046                          | 0.732                          | 15.973                      | I          |              |
| C-R-225-5×5 | 225        | 16.733         | 20.283         | 0.521                          | 0.186                          | 0.357                       | I          |              |
| C-R-235-5×5 | 235        | 15.743         | 24.233         | 0.332                          | 0.240                          | 0.721                       | I          |              |
| C-R-240-5×5 | 240        | 22.767         | 31.007         | 0.346                          | 0.394                          | 1.137                       | 1.183      | I            |
| C-R-245-5×5 | 245        | 25.580         | 28.057         | 0.219                          | 0.500                          | 2.280                       | I          |              |
| C-R-250-5×5 | 250        | 30.457         | 41.489         | 0.041                          | 0.671                          | 16.238                      | I          |              |
| C-R-225-7×7 | 225        | 20.013         | 23.480         | 0.625                          | 0.222                          | 0.356                       | I          |              |
| C-R-235-7×7 | 235        | 22.887         | 24.317         | 0.486                          | 0.348                          | 0.715                       | I          |              |
| C-R-240-7×7 | 240        | 26.467         | 27.620         | 0.404                          | 0.457                          | 1.133                       | 1.548      | I            |
| C-R-245-7×7 | 245        | 34.400         | 34.930         | 0.297                          | 0.671                          | 2.258                       | I          |              |
| C-R-250-7×7 | 250        | 34.339         | 39.770         | 0.048                          | 0.756                          | 15.878                      | I          |              |

$^3$L$_R$ – Length of the rock block; $P_{ini}$ – Initial cracking load; $P_{max}$ – Peak load; $K_{ini}^{IC}$ – Initial fracture toughness of mode 1; $K_{ini}^{IC}$ – Initial fracture toughness of mode 2; $R_e$ – Degree of roughness; Failure mode “I” – Interfacial crack propagates through the interface; Failure mode “IC” – Sudden brittle failure near the supports at the same time when the interfacial crack propagates through the whole interface.

Table 4 Experimental results of the R-C series beams under FPS$^4$.

| Specimen   | $L_R$ (mm) | $P_{ini}$ (kN) | $P_{max}$ (kN) | $K_{ini}^{IC}$ (MPa·m$^{1/2}$) | $K_{ini}^{IC}$ (MPa·m$^{1/2}$) | $|K_{ini}^{IC}/K_{ini}^{IC}|$ | $R_e$ (mm) | Failure mode |
|------------|------------|----------------|----------------|--------------------------------|--------------------------------|-----------------------------|------------|--------------|
| R-C-264-4×4 | 264        | 17.737         | 22.300         | 0.360                          | 0.284                          | 0.788                       | 0.963      | K            |
| R-C-266-4×4 | 266        | 17.461         | 20.360         | 0.394                          | 0.274                          | 0.696                       | I          |              |
| R-C-271-5×5 | 271        | 13.552         | 16.710         | 0.378                          | 0.201                          | 0.531                       | 1.183      | K            |
| R-C-275-5×5 | 275        | 12.640         | 13.380         | 0.404                          | 0.176                          | 0.437                       | I          |              |

$^4$L$_R$ – Length of the rock block; $P_{ini}$ – Initial cracking load; $P_{max}$ – Peak load; $K_{ini}^{IC}$ – Initial fracture toughness of mode 1; $K_{ini}^{IC}$ – Initial fracture toughness of mode 2; $R_e$ – Degree of roughness; Failure mode “I” – Propagation of the interfacial crack through the interface; Failure mode “K” – Initiation and propagation of the crack in the concrete.
Figures

(a) Under three-point bending (TPB)

(b) Under four-point shear (FPS)

Fig. 1. Geometries of TPB and C-R series specimens for TPB and FPS fracture tests

(a) PVC film 1 pasted on the rock   (b) PVC film 2 fixed using cello tape

Fig. 2. Preparation of the pre-crack

(a) 3×3   (b) 4×4   (c) 5×5   (d) 7×7   (e) $R_a/M_{size}$

Fig. 3. Features of rock surfaces at the interface
Fig. 4. Experimental setups

Fig. 5. Load versus strain curve for Specimen C-R-240-4×4-1

Fig. 6. Failure modes of C-R series specimens under FPS
**Fig. 7.** Cross-section of the specimen under interfacial failure

**Fig. 8.** $K_1$ versus $K_2$ relationships for interface crack initiation at four roughness degrees

**Fig. 9.** Normalised $K_1$ versus $K_2$ relationships at interface crack initiation
Fig. 10. Cohesive tensile/shear stress versus displacement relationships

Fig. 11. Flow chart for numerical simulations
(a) Specimen TPB-5×5

(b) Specimen C-R-240-3×3

(c) Specimen C-R-240-4×4
Fig. 12. Comparisons of $P$-$CMOD$ curves with the test data on TPB and C-R series specimens.
(a) Curves for the rock with $K_{1,II}^* = K_{1j}^{ini}$ and $K_{1,2}^* = K_{1C}^{ini}$

(b) Curves for the concrete with $K_{1,II}^* = K_{1j}^{ini}$ and $K_{1,2}^* = K_{1C}^{ini}$

**Fig. 13.** $K_1$ versus $K_2$ relationships for crack propagation criteria $K_{1,II}^* = K_{1j}^{ini}$ and $K_{1,2}^* = K_{1C}^{ini}$

**Fig. 14.** Geometries of R-C series beams under four-point shear (FPS)
Fig. 15. Failure mode K of typical beams

Fig. 16. Comparisons of numerical $P$-$CMOD$ curve and crack trajectory with the test data